## Calculus

## Practice Test 2

Problem 1.- An input tray is a box open at one side, where people can put envelopes to be processed. It is built out of a sheet of metal, as shown in the figure. The squares at the corners are cut out and the flaps folded to make the tray. Calculate the value of $x$, so the tray contains the most possible volume.


Problem 2.- Use the L'Hospital rule to find the following limits if they exist.
a) $\operatorname{Lim}_{x \rightarrow 0} \ln (1-\cos x)-\ln x^{2}$
b) $\operatorname{Lim}_{x \rightarrow \infty} \frac{1+5 x^{2}+4 x^{3}}{1+5 x+4 x^{2}}$

Problem 3.- Maxima and minima. Find the maxima and minima of the following function

$$
f(x)=2 x^{3}+3 x^{2}-36 x+5
$$

Problem 4.- Use Newton's method to find a solution to the equation between $x=1$ and 2 .
$5+4 \cos x-3 x=0$

Problem 5.- Calculate the antiderivative of the function $\quad f(x)=\sec ^{2} x+\sec x \tan x$

Problem 6.- Sketch the derivative of the function shown in the graph


