## Electromagnetism

## **Faraday law**

**Problem 1.-** A solenoid is being wound around a plastic cylinder of radius R. There is a magnetic field of magnitude B parallel to the axis of the cylinder. Calculate the emf induced between the open ends of the wire knowing that the rate of winding is N turns per second.



**Solution:** Faraday's law:  $emf = -\frac{d\phi}{dt} = -\frac{dNBA\sin \angle_A^B}{dt} = -NB\pi R^2$ 

**Problem 2.-** A copper ring has a resistance  $R=0.15\Omega$ , a radius r=0.25m and is in a constant magnetic field B=0.9 tesla perpendicular to the plane of the ring. Then, the magnetic field is reduced to zero, which induces a current in the ring. Calculate the total charge that passes through a given point in the ring.



Solution: 
$$emf = IR = \frac{dQ}{dt}R = \frac{d\phi}{dt} \rightarrow Q = \frac{\Delta\phi}{R} = \frac{NBA}{R} = \frac{0.9 \times \pi \times 0.25^2}{0.15} = 1.18 \text{ C}$$

**Problem 3.-** Consider a solar panel that has a length of 40m in orbit moving at a speed of 7,900 m/s. Calculate the voltage difference between the ends of the panel if the magnetic field of the earth at a certain instant is  $30\mu$ T and makes 90 degrees with the panel and its velocity.



**Solution:**  $emf = BvL = (30 \times 10^{-6}T)(7900m/s)(40m) = 9.48$  volts

**Problem 4.-** A circuit is built by connecting a resistance  $R=2\Omega$  to a conducting wire in the shape of a U with width w = 0.5 m, and a sliding conducting bar that closes the circuit. Consider that this circuit is in a region where the magnetic field is B = 1 T perpendicular to the plane of the circuit and the resistances of the wire and bar are negligible.



a) Calculate the *emf* if the bar moves to the right at a speed v = 10m/s

b) Calculate the induced current in case (a). Is the direction indicated in the drawing correct?

c) Calculate the speed v necessary to induce a current of 0.5 A

d) Is it reasonable to ignore the magnetic field created by the induced current in each case?