

Physics I

Ideal Gases

$$R = 8.314 \frac{\text{J}}{\text{Kmol}}, \quad k_B = 1.38 \times 10^{-23} \text{ J/K}, \quad 1 \text{ atm} = 1.013 \times 10^5 \text{ pascals}$$

$$T_{\text{Kelvin}} = T_{\text{Celsius}} + 273.15 \quad PV = nRT \quad \text{or} \quad PV = Nk_B T$$

Problem 1.- How much mass of helium is contained in a 50.0 L cylinder at a pressure of 10.0 atm and a temperature of 35.0 °C?

[The atomic mass of helium is 4 amu]

Solution: The number of moles is: $n = \frac{PV}{RT} = \frac{(10 \times 1.013 \times 10^5)(0.05)}{8.314 \times (273 + 35)} = 19.78$

The mass is $m = nM = 19.78 \times 0.004 \text{ kg} = \mathbf{0.079 \text{ kg}}$

Problem 2.- A tank of compressed oxygen is at a temperature of 27 °C and a pressure of 2,500 kPa. Calculate the mass of oxygen contained in the tank if its volume is 0.12 m³.

[The molecular mass of O₂ is 32]

Solution: First, we calculate the number of moles:

$$pV = nRT \rightarrow n = \frac{pV}{RT}$$

$$p = 2,500 \text{ kPa} = 2,500 \times 10^3 \text{ Pa}$$

$$T = 27 + 273 = 300 \text{ K}$$

$$V = 0.12 \text{ m}^3$$

$$R = 8.314 \text{ J/K}$$

$$\rightarrow n = \frac{pV}{RT} = \frac{(2500 \times 10^3 \text{ Pa})(0.12 \text{ m}^3)}{8.314 \text{ J/K}(300 \text{ K})} = 120 \text{ moles}$$

Since each mole is 32 grams:

$$\text{Mass of oxygen} = 120 \times 32 \text{ g} = \mathbf{3.85 \text{ kg}}$$

Problem 3.- Calculate the molecular weight of a gas if 35.4 g of the gas stored in a 7.50 L tank exerts a pressure of 60.0 atm at a constant temperature of 45.5 °C

Solution:

$$V = 7.5 \text{ L} = 7.5 \times 10^{-3} \text{ m}^3$$

$$T = 45.5 + 273.15 = 318.65 \text{ K}$$

$$P = 60 \text{ atm} \left(\frac{1.013 \times 10^5 \text{ pascals}}{1 \text{ atm}} \right) = 60.8 \times 10^5 \text{ pascals}$$

$$\text{With these values: } n = \frac{PV}{RT} = \frac{(60.8 \times 10^5)(7.5 \times 10^{-3})}{8.314(318.65)} = \mathbf{17.2 \text{ moles}}$$

$$\text{So, the molecular mass is } M = \frac{35.4}{17.2} = \mathbf{2.05}$$

Problem 4.- How many moles of gas are contained in 890.0 mL at 21.0 °C and 750.0 mm Hg pressure?

Solution: The problem provides the following information:

$$V = 890\text{mL} = 890\text{mL} \left(\frac{1\text{L}}{1000\text{mL}} \right) \left(\frac{1\text{m}^3}{1000\text{L}} \right) = 890 \times 10^{-6} \text{m}^3$$

$$T = 21 + 273 = 294\text{K}$$

$$P = 750\text{mmHg} = 750\text{mmHg} \left(\frac{1\text{atm}}{760\text{mmHg}} \right) \left(\frac{1.013 \times 10^5 \text{ pascals}}{1\text{atm}} \right) = 0.999 \times 10^5 \text{ pascals}$$

With these values:

$$n = \frac{PV}{RT} = \frac{(0.999 \times 10^5)(890 \times 10^{-6})}{8.314(294)} = \mathbf{0.036 \text{ moles}}$$

Problem 5.- 1.09 g of H₂ is contained in a 2.00 L container at 20.0 °C. What is the pressure in this container in mm Hg?

Solution: The number of moles is: $n = \frac{\text{mass}}{\text{molecular mass in grams}} = \frac{1.09\text{g}}{2\text{g}} = 0.545$

$$V = 2\text{L} = 2\text{L} \left(\frac{1\text{m}^3}{1000\text{L}} \right) = 2 \times 10^{-3} \text{m}^3$$

$$T = 20 + 273 = 293\text{K}$$

$$\text{So, the pressure is: } P = \frac{nRT}{V} = \frac{(0.545)(8.314)(293)}{2 \times 10^{-3}} = 6.64 \times 10^5 \text{ pascals}$$

In mmHg:

$$P = 6.64 \times 10^5 \text{ pascal} \left(\frac{1\text{atm}}{1.013 \times 10^5 \text{ pascals}} \right) \left(\frac{760\text{mmHg}}{1\text{atm}} \right) = \mathbf{5,000 \text{ mmHg}}$$

Problem 6.- Calculate the volume 3.00 moles of a gas will occupy at 24.0 °C and 762.4 mm Hg.

Solution: $n = 3$

$$T = 24 + 273 = 297\text{K}$$

The pressure is:

$$P = 762.4\text{mmHg} = 762.4\text{mmHg} \left(\frac{1\text{atm}}{760\text{mmHg}} \right) \left(\frac{1.013 \times 10^5 \text{ pascals}}{1\text{atm}} \right) = 1.016 \times 10^5 \text{ pascals}$$

And the volume is:

$$V = \frac{nRT}{P} = \frac{3(8.314)(297)}{1.016 \times 10^5} = \mathbf{0.073 \text{ m}^3}$$

Problem 7.- What volume will 20.0 g of Argon occupy at STP?

$$\text{Solution: } n = \frac{\text{mass}}{\text{molecular mass in grams}} = \frac{20\text{g}}{40\text{g}} = 0.5$$

STP stands for:

$$P = 1\text{atm} = 1.013 \times 10^5 \text{ pascals}, T = 0\text{C} = 273\text{K}, \text{ so the volume is:}$$

$$V = \frac{nRT}{P} = \frac{0.5(8.314)(273)}{1.013 \times 10^5} = \mathbf{0.011 \text{ m}^3}$$

Problem 8.- How many moles of gas would be present in a gas trapped within a 100.0 mL vessel at 25.0 °C at a pressure of 2.50 atmospheres?

Solution: The information given:

$$V = 100\text{mL} = 100\text{mL} \left(\frac{1\text{L}}{1000\text{mL}} \right) \left(\frac{1\text{m}^3}{1000\text{L}} \right) = 1 \times 10^{-4} \text{ m}^3$$

$$T = 25 + 273 = 298\text{K}$$

$$P = 2.50\text{atm} = 2.5\text{atm} \left(\frac{1.013 \times 10^5 \text{ pascals}}{1\text{atm}} \right) = 2.53 \times 10^5 \text{ pascals}$$

With these values:

$$n = \frac{PV}{RT} = \frac{(2.53 \times 10^5)(1 \times 10^{-4})}{8.314(298)} = \mathbf{0.0102 \text{ moles}}$$

Problem 9.- How many moles of a gas would be present in a gas trapped within a 37.0-liter vessel at 80.00 °C at a pressure of 2.50 atm?

$$\text{Solution: } V = 37\text{L} = 37\text{L} \left(\frac{1\text{m}^3}{1000\text{L}} \right) = 37 \times 10^{-3} \text{ m}^3$$

$$T = 80 + 273 = 353\text{K}$$

$$P = 2.50\text{atm} = 2.5\text{atm} \left(\frac{1.013 \times 10^5 \text{ pascals}}{1\text{atm}} \right) = 2.53 \times 10^5 \text{ pascals}$$

With these values:

$$n = \frac{PV}{RT} = \frac{(2.53 \times 10^5)(37 \times 10^{-3})}{8.314(353)} = \mathbf{3.2 \text{ moles}}$$

Problem 10.- If the number of moles of a gas is doubled at the same temperature and pressure, will the volume increase or decrease?

Solution: It will double!

Problem 11.- What volume will 1.27 moles of helium gas occupy at STP?

Solution: $n = 1.27$

STP stands for:

$P = 1\text{atm} = 1.013 \times 10^5 \text{ pascals}$, $T = 0\text{C} = 273\text{K}$, so the volume is:

$$V = \frac{nRT}{P} = \frac{1.27(8.314)(273)}{1.013 \times 10^5} = \mathbf{0.028 \text{ m}^3}$$

Problem 12.- At what pressure would 1.50 mole of nitrogen gas at 23.0 °C occupy 8.90 L?

Solution: $n=1.5$

$$V = 8.9\text{L} = 8.9\text{L} \left(\frac{1\text{m}^3}{1000\text{L}} \right) = 8.9 \times 10^{-3} \text{m}^3$$

$$T = 23 + 273 = 296\text{K}$$

With these values:

$$P = \frac{nRT}{V} = \frac{1.5(8.314)(296)}{8.9 \times 10^{-3}} = \mathbf{414,000 \text{ pascals}}$$

Problem 13.- What volume would 32.0 g of NO₂ gas occupy at 3.12 atm and 18.0 °C?

Solution: The number of moles is: $n = \frac{\text{mass}}{\text{molecular mass in grams}} = \frac{32\text{g}}{44\text{g}} = 0.727$

$$T = 18 + 273 = 291\text{K}$$

The pressure is: $P = 3.12\text{atm} \left(\frac{1.013 \times 10^5 \text{ pascals}}{1\text{atm}} \right) = 3.16 \times 10^5 \text{ pascals}$

So, the volume is: $V = \frac{nRT}{P} = \frac{0.727(8.314)(291)}{3.16 \times 10^5} = \mathbf{0.0055 \text{ m}^3}$

Problem 14.- Find the volume of 2.40 mol of gas whose temperature is 50.0 °C and whose pressure is 2.00 atm.

Solution: The number of moles is: $n = 2.4$

$$T = 50 + 273 = 323\text{K}$$

The pressure is: $P = 2\text{atm} \left(\frac{1.013 \times 10^5 \text{ pascals}}{1\text{atm}} \right) = 2.026 \times 10^5 \text{ pascals}$

Then, the volume is: $V = \frac{nRT}{P} = \frac{2.4(8.314)(323)}{2.026 \times 10^5} = \mathbf{0.0347\text{m}^3}$

Problem 15.- Calculate the molecular weight of a gas if 35.44 g of the gas stored in a 7.50 L tank exerts a pressure of 60.0 atm at a constant temperature of 35.5 °C

Solution: Let us find the number of moles:

$$V = 7.5L = 7.5L \left(\frac{1m^3}{1000L} \right) = 7.5 \times 10^{-3} m^3$$

$$T = 35.5 + 273 = 308.5K$$

$$P = 60atm = 60atm \left(\frac{1.013 \times 10^5 \text{ pascals}}{1atm} \right) = 60.78 \times 10^5 \text{ pascals}$$

With these values:

$$n = \frac{PV}{RT} = \frac{(60.78 \times 10^5)(7.5 \times 10^{-3})}{8.314(308.5)} = \mathbf{17.8 \text{ moles}}$$

And the molecular weight is 35.44 g/17.8 = **1.99**, so it could be hydrogen.

Problem 16.- How many moles of gas are contained in a 50.0 L cylinder at a pressure of 100.0 atm and a temperature of 35.0 °C?

$$\mathbf{Solution:} \quad V = 50L = 50L \left(\frac{1m^3}{1000L} \right) = 50 \times 10^{-3} m^3$$

$$T = 35 + 273 = 308K$$

$$P = 100atm = 100atm \left(\frac{1.013 \times 10^5 \text{ pascals}}{1atm} \right) = 101.3 \times 10^5 \text{ pascals}$$

With these values:

$$n = \frac{PV}{RT} = \frac{(101.3 \times 10^5)(50 \times 10^{-3})}{8.314(308)} = \mathbf{198 \text{ moles}}$$

Problem 17.- Determine the number of moles of Krypton contained in a 3.25-liter gas tank at 5.80 atm and 25.5 °C. If the gas is Oxygen instead of Krypton, will the answer be the same? Why or why not?

$$\mathbf{Solution:} \quad n = \frac{PV}{RT} = \frac{(5.8 \times 1.013 \times 10^5 \text{ pascals})(3.25 \times 10^{-3} m^3)}{8.314(298.65K)} = \mathbf{0.769 \text{ moles}}$$

Oxygen at those conditions would give us the same value. Notice that the equation does not contain the mass.

Problem 18.- Determine the number of grams of carbon dioxide in a 450.6 mL tank at 1.80 atm and minus 50.5 °C. Determine the number of grams of oxygen that the same container will contain under the same temperature and pressure.

$$\text{Solution: } n = \frac{PV}{RT} = \frac{(1.8 \times 1.013 \times 10^5 \text{ pascals})(0.4506 \times 10^{-3} \text{ m}^3)}{8.314(273.15 - 50.5)} = \mathbf{0.0444 \text{ moles}}$$

The mass is: $0.0444 \times 44 \text{ g} = \mathbf{1.95 \text{ g}}$

If it were oxygen, the mass would be $0.0444 \times 32 = \mathbf{1.42 \text{ g}}$

Problem 19.- Determine the volume of occupied by 2.34 grams of carbon dioxide gas at STP.

$$\text{Solution: } V = \frac{nRT}{p} = \frac{\left(\frac{2.34}{44}\right) 8.314(273.15)}{1.013 \times 10^5 \text{ pascals}} = \mathbf{0.00119 \text{ m}^3}$$

Problem 20.- A sample of argon gas at STP occupies 56.2 liters. Determine the number of moles of argon and the mass in the sample.

$$\text{Solution: } n = \frac{56.2}{22.4} = \mathbf{2.509}$$

$$\text{Mass} = 2.509 \times 40 = \mathbf{100.35 \text{ g}}$$

Problem 21.- At what temperature will 0.654 moles of neon gas occupy 12.30 liters at 1.95 atmospheres?

$$\text{Solution: } T = \frac{pV}{nR} = \frac{(1.95 \times 1.013 \times 10^5 \text{ pascals})(12.3 \times 10^{-3})}{0.654 \times 8.314} = \mathbf{446.8 \text{ K}}$$

Problem 22.- A 30.6 g sample of gas occupies 22.4 L at STP. What is the molecular weight of this gas?

Solution: It is $\mathbf{30.6}$

Problem 23.- A 40.0 g gas sample occupies 11.2 L at STP. Find the molecular weight of this gas.

Solution: It is $\mathbf{80.0}$

Problem 24.- A 12.0 g sample of gas occupies 19.2 L at STP. What is the molecular weight of this gas?

$$\text{Solution: } n = \frac{19.2}{22.4} = 0.857, \text{ so } M = 12.0 / 0.857 = \mathbf{14}$$

Problem 25.- 96.0 g. of a gas occupies 48.0 L at 700.0 mm Hg and 20.0 °C. What is its molecular weight?

Solution: $n = \frac{PV}{RT} = \frac{(700/760 \times 1.013 \times 10^5 \text{ pascals})(48 \times 10^{-3} \text{ m}^3)}{8.314(293.15 \text{ K})} = \mathbf{1.83 \text{ moles}}$

$M = 96.0/1.83 = \mathbf{48.98}$

Problem 26.- 20.83 g. of a gas occupies 4.167 L at 79.97 kPa at 30.0 °C. What is its molecular weight?

Solution: $n = \frac{PV}{RT} = \frac{(79.97 \times 10^3 \text{ pascals})(4.167 \times 10^{-3} \text{ m}^3)}{8.314(313.15 \text{ K})} = \mathbf{0.128 \text{ moles}}$

$M = 20.83/0.128 = \mathbf{162.7}$

Problem 27.- At STP 3.00 liters of an unknown gas has a mass of 9.50 grams. Calculate its molar mass.

Solution: $n = \frac{3}{22.4} = 0.1339$, so $M = 9.50/0.1339 = \mathbf{70.9}$

Problem 28.- At STP 0.250 liter of an unknown gas has a mass of 1.00 gram. Calculate its molar mass.

Solution: $n = \frac{0.25}{22.4} = 0.0111$, so $M = 1/0.0111 = \mathbf{89.6}$

Problem 29.- At STP 150.0 mL of an unknown gas has a mass of 0.250 gram. Calculate its molar mass.

Solution: $n = \frac{0.150}{22.4} = 0.006696$, so $M = 0.25/0.006696 = \mathbf{37.3}$

Problem 30.- 1.089 g of a gas occupies 4.50 L at 20.5 °C and 0.890 atm. What is its molar mass?

Solution: $n = \frac{PV}{RT} = \frac{(0.89 \times 1.013 \times 10^5 \text{ pascals})(4.5 \times 10^{-3} \text{ m}^3)}{8.314(293.65 \text{ K})} = 0.166 \text{ moles}$

So, $M = 1.089/0.166 = \mathbf{6.55}$

Problem 31.- 0.190 g of a gas occupies 250.0 mL at STP. What is its molar mass? What gas is it? Hint - calculate molar mass of the gas.

Solution: $n = \frac{0.25}{22.4} = 0.0111$, so $M = 0.19/0.0111 = \mathbf{17... \text{ could be ammonia}}$

Problem 32.- If 9.006 grams of a gas are enclosed in a 50.00-liter vessel at 273.15 K and 2.000 atmospheres of pressure, what is the molar mass of the gas? What gas is this?

Solution: $n = \frac{PV}{RT} = \frac{(2 \times 1.013 \times 10^5 \text{ pascals})(50 \times 10^{-3} \text{ m}^3)}{8.314(273.15 \text{ K})} = 4.46 \text{ moles}$

$M = 9.006 / 4.46 = 2$ **It is hydrogen.**

Problem 33.- A 50.00-liter tank at minus 15.00 °C contains 14.00 grams of helium gas and 10.00 grams of nitrogen gas.

- Determine the moles of helium gas in the tank.
- Determine the moles of nitrogen gas in the tank.
- Determine the mole fraction of helium gas in the tank.
- Determine the partial pressure of helium gas in the tank.
- Determine the partial pressure of nitrogen gas in the tank.
- Determine the total pressure of the mixture in the tank.
- Determine the volume that the mixture will occupy at STP.

Problem 34.- Determine the number of moles of Krypton contained in a 3.25-liter gas tank at 5.80 atm and 25.5 °C. If the gas is Oxygen instead of Krypton, will the answer be the same? Why or why not?

[1 atm=101,300 pascal]

Solution: The number of moles is $n = \frac{PV}{RT} = \frac{5.8 \times 1.013 \times 10^5 \times 0.00325}{8.314 \times 298.5} = 0.77 \text{ moles}$

The same answer if it were oxygen instead of krypton because the law is universal for all ideal gasses.

Problem 35.- A compressed cylinder of O₂ contains 30 kg of oxygen at T=25°C and 10⁶ pascals. Calculate the volume of the cylinder.

Solution: We can use the ideal gas law: $pV = nRT \rightarrow V = \frac{nRT}{p}$

The number of moles is: $n = \frac{30,000 \text{ g}}{32 \text{ g}} = 937.5 \text{ moles}$

So the volume is:

$\rightarrow V = \frac{937.5(8.314 \text{ J/K})(298 \text{ K})}{10^6 \text{ Pa}} = 2.32 \text{ m}^3$

Problem 35a.- A compressed cylinder of O₂ contains 6.4 kg of oxygen at T=26.85°C and P=6atm. Calculate the volume of the cylinder. [The molecular weight of oxygen is 32]

Solution: The number of moles is: $n = \frac{\text{mass(in grams)}}{\text{Molecular mass}} = \frac{6400}{32} = 200 \text{ moles}$

The temperature is: $T = 26.85 + 273.15 = 300 \text{ K}$

The pressure is: $P = 6atm \left(\frac{1.013 \times 10^5 \text{ pascals}}{atm} \right) = 6.78 \times 10^5 \text{ pascals}$,

So the volume is: $V = \frac{nRT}{P} = \frac{200 \times 8.314 \times 300}{6.078 \times 10^5} = \mathbf{0.82 \text{ m}^3}$

Problem 36.- A diver releases a 1cm-radius air bubble at a depth of 45m (so you can consider the absolute pressure to be 5.5 atm) at a temperature of 7°C. Calculate the radius of the bubble just before it surfaces (where the pressure is 1.0 atm) if the temperature is 17°C.

[Volume of a sphere = $\frac{4}{3} \pi R^3$, where R is the radius]

Solution: The number of moles stays the same in the process, so $\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$, and according to

the problem:

$$P_1 = 5.5atm$$

$$T_1 = 7 + 273.15 = 280.15K$$

$$V_1 = \frac{4}{3} \pi R_1^3$$

Notice that we are leaving the pressure in atm as those units will cancel each other.

Also:

$$P_2 = 1atm$$

$$T_2 = 17 + 273.15 = 290.15K$$

$$V_2 = \frac{4}{3} \pi R_2^3$$

$$\text{So, } \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \rightarrow \frac{5.5 \times \frac{4}{3} \pi R_1^3}{280.15} = \frac{1 \times \frac{4}{3} \pi R_2^3}{290.15} \rightarrow R_2 = R_1 \sqrt{\frac{5.5 \times 290.15}{280.15}} = \mathbf{1.79 \text{ cm}}$$