

Physics I

Velocity Calculus

Definition of velocity in one dimension: $v = \frac{dx}{dt}$

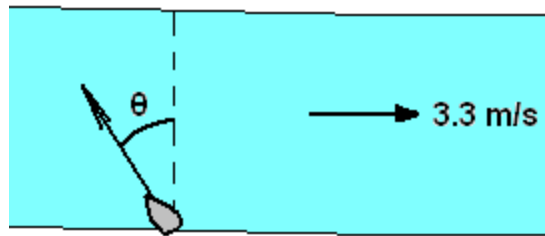
Definition of acceleration in one dimension: $a = \frac{dv}{dt} = \frac{d^2x}{dt^2}$

Problem 1.- A satellite in polar orbit moves towards the north at 8,550 m/s when it collides with another satellite in equatorial orbit, which at that point was moving towards the east at 8,250 m/s. Calculate the speed of the second satellite with respect to the first.

Problem 2.- An oil droplet of mass m is falling in air and experiences a drag force equal to $-bv$ where b is a constant proportional to the viscosity of air. Calculate its terminal velocity and its kinetic energy when that velocity is reached.

[Ignore buoyancy]

Problem 3.- A person wants to cross a river with a motorboat that has a speed of 5.5 m/s, however, the water current has a speed of 3.3 m/s. Calculate the angle needed to get straight to the other side.



Problem 4.- A projectile with initial velocity v_0 enters a viscous fluid where the acceleration is given by: $a = -kv^2$, find the velocity as a function of time.

Useful integral: $\int \frac{dx}{x^2} = -\frac{1}{x} + C$

Problem 5.- An object dropped on Titan (Saturn's largest moon) is attracted to the surface with an acceleration equal to: $a = g_{\text{Titan}} - kv$

Where $g_{\text{Titan}} = 1.35 \frac{m}{s^2}$ is the acceleration due to gravity and $k = 0.033s^{-1}$ is a resistance due to the viscosity of Titan's dense atmosphere.

Find the terminal velocity of the object.

Problem 6.- A small object falls with initial velocity $v_o=1.5\text{m/s}$ in a viscous fluid where the acceleration is given by: $a = g - 25v$, find the terminal velocity and sketch the velocity as a function of time.

Problem 7.- If the position of a 2.5 kg particle is described by the vector:

$$\vec{r} = (t, 5 \sin t)$$

Find the net force acting on the particle.

Problem 8.- A particle moves in a straight line following the equation:

$$x = 8t^2 + 5t + 1$$

Determine the position, velocity, and acceleration at $t = 2.0$ s.

Problem 9.- A particle follows a trajectory described by the equation:

$$x(t) = 25t^3 + 5t^2 + 20$$

Where t is the time in seconds, find the velocity and acceleration at $t=2$ seconds.

Problem 10.- A particle has a velocity described by the equation:

$$v(t) = 5t^3$$

Where t is the time in seconds, find the displacement from $t_1 = 1$ to $t_2 = 5$ seconds

Problem 11.- A particle follows a trajectory described by the equation:

$$x(t) = 1.5t^3 + 0.5t + 1$$

Where t is the time in seconds, find the velocity and acceleration as a function of time.

Problem 12.- The acceleration of a falling object in a viscous fluid is given by $a=Ae^{-bt}$, calculate the velocity as a function of time if the initial velocity is V_o

Problem 13.- A particle follows a trajectory described by the equation $x = 5 + 8t - t^2$

- Calculate the instantaneous velocity of the particle.
- Find at what time the velocity is zero.
- Using the time calculated in (b) calculate the maximum value of x .

Problem 14.- The position of a particle is given by $x=10t^3+3$, $y=5t^2-14t$, where x and y are in meters and t is in seconds. Find the instantaneous acceleration of the particle at $t=2$ seconds.

Problem 15.- The position of a particle is given by $x=8t+3$, $y=9t^2-14t$. Find the average velocity of the particle between $t=2$ s and $t=5$ s.

Problem 16.- A particle follows a trajectory described by the equation:

$$x(t) = \frac{A}{t^2 + b}$$

Find the velocity as a function of time.