

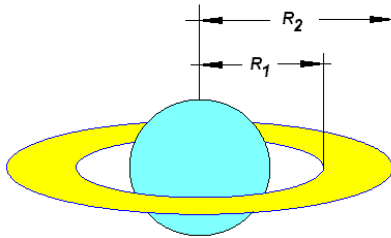
Physics I

Kepler's Laws

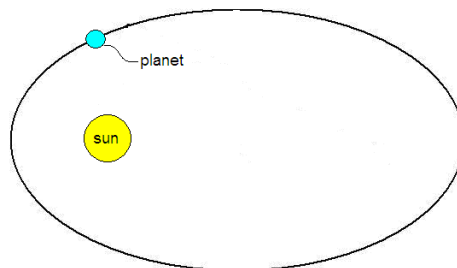
Kepler's third law:

$$\frac{R_1^3}{T_1^2} = \frac{R_2^3}{T_2^2}$$

Problem 1.- A planet has a ring of particles describing circular orbits. The outer part of the ring has a radius $R_2=27,500$ km and a period of 12.5 days. Calculate the period of the particles in the inner part of the ring where the radius is $R_1=17,600$ km



Problem 2.- Indicate at what point in the elliptical orbit the planet has its maximum kinetic energy. Give a rationale for your answer.



Problem 3.- A satellite of mass m orbits a planet of mass M in a circular orbit with radius R . The time required for one revolution is

- (A) independent of M
- (B) proportional to m
- (C) linear in R
- (D) proportional to $R^{3/2}$
- (E) proportional to R^2

Problem 4.- Callisto is one of the moons of Jupiter that was discovered by Galileo. It has a period of 16.7 days and a mean distance from Jupiter of 1.883×10^6 km. Calculate the period of Io, which is also a moon of Jupiter, knowing that its mean distance to Jupiter is 0.422×10^6 km.

Problem 5.- An artificial satellite in orbit around our planet needs 12 hours to complete one revolution. Calculate the radius of the circular orbit knowing that the period of a satellite in low earth orbit (LEO) is approximately 90 minutes.

LEO is an orbit so close to the Earth that you can say that the radius of the orbit is equal to the radius of the earth R_E .

Problem 6.- Calculate how long the Martian year is, knowing that its average distance to the Sun is 228×10^6 km.

Earth's year is 365.25 days and the distance from the Earth to the Sun is 150×10^6 km.